



## Form Measurement

**AMETEK**  
ULTRA PRECISION TECHNOLOGIES

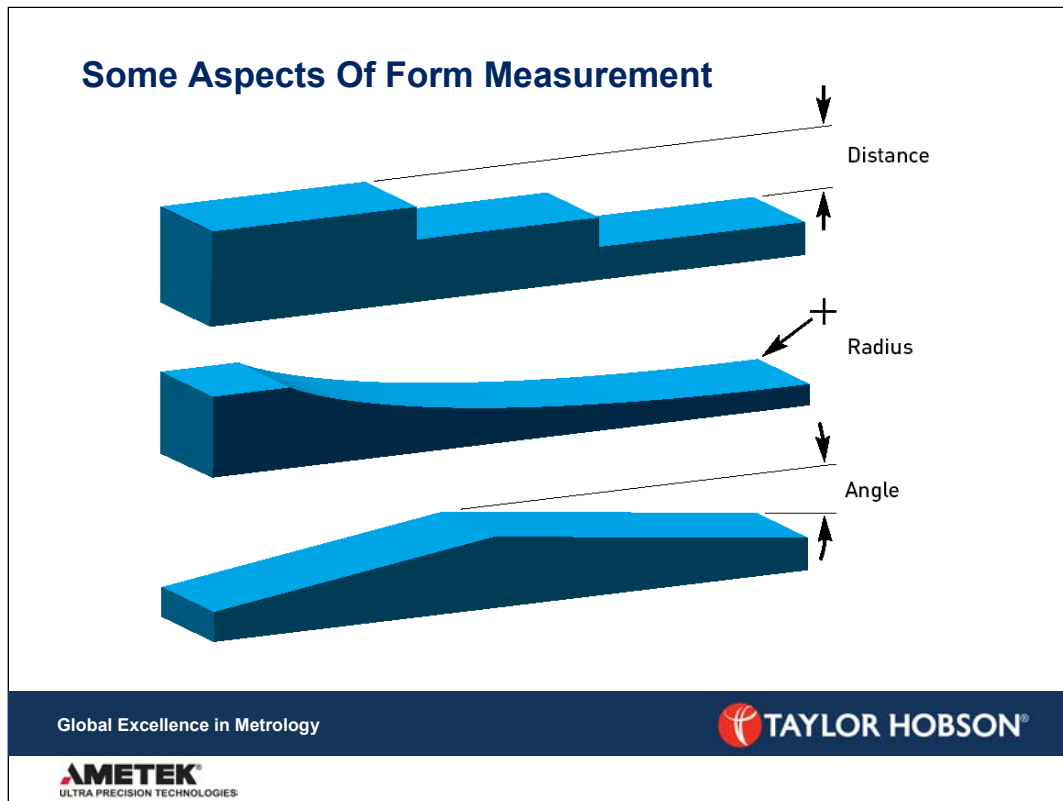
## Contents

- Aspects of Form Measurement
- Form Fit - Least Squares Line
  - Straightness LS Line
  - Straightness MZ line
- Form Fit - Least Squares Arc
- Accuracy of Radius Measurement
  - Example
- Form Exclusions
  - Example
- Dimensional Measurement
  - Example

Global Excellence in Metrology



**AMETEK**  
ULTRA PRECISION TECHNOLOGIES



Gauge Range, Resolution and Linearity are important for Form Measurement.

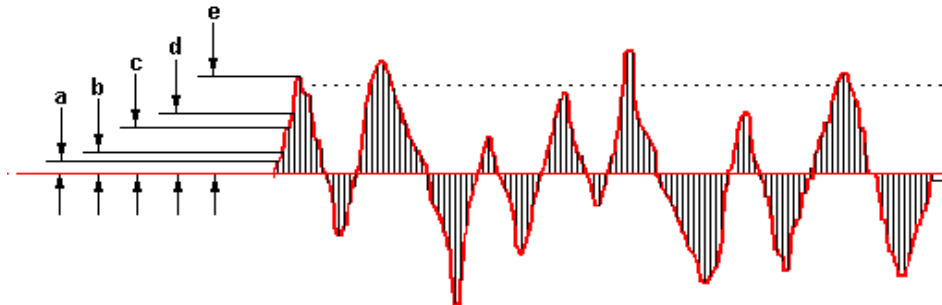
Often, a large range and excellent resolution are required.

This means that the calibration method is very important.

Some considerations are:

- a) Gauge range , Resolution and Linearity
- b) Calibration Method / Ball Radius
- c) Stylus Type & ensure Stylus tip is suitable
- d) Ensure measurement is within the calibrated range
- e) Ensure part does not contact the stylus tip at a position which was not covered by the calibration. This means that the stylus length, the stylus tip radius and the calibration ball radius must be considered.
- f) Ensure stylus does not 'flank'
- g) Component alignment and fixturing.

## Form Fit : Least Squares Line



$$a^2 + b^2 + c^2 + d^2 + \dots = \text{minimum}$$

Global Excellence in Metrology

 TAYLOR HOBSON®

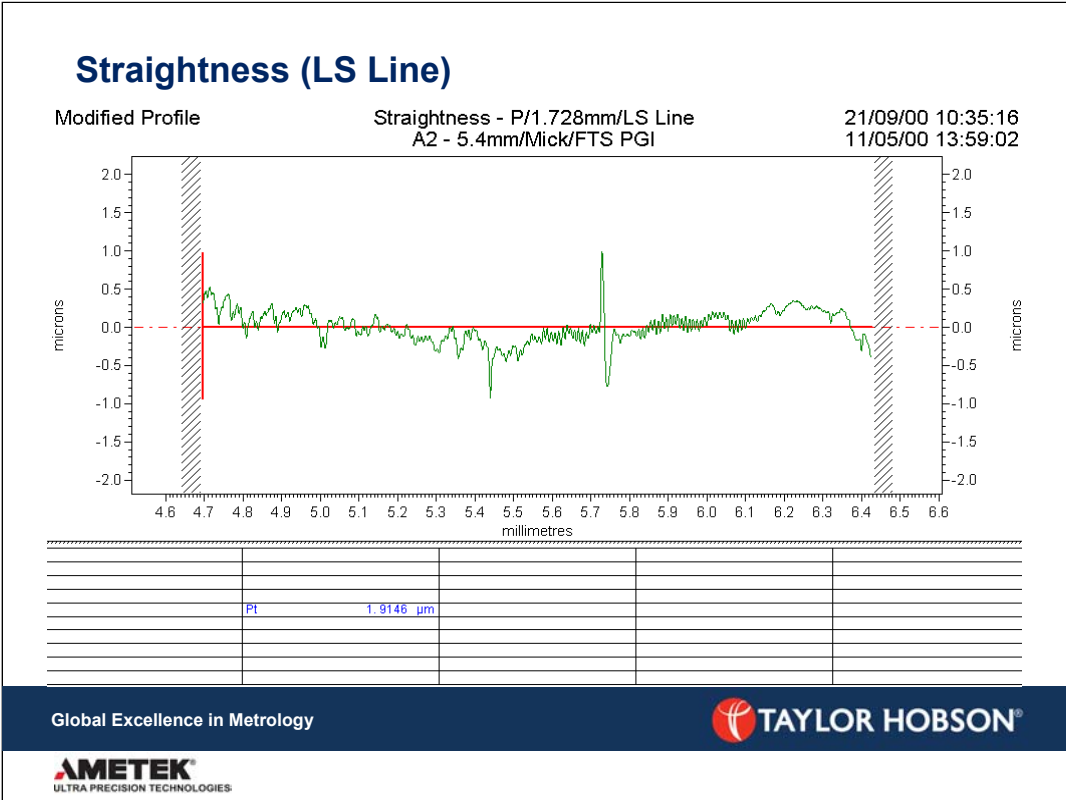
 **AMETEK**  
ULTRA PRECISION TECHNOLOGIES

Parameters such as peak to valley need to be related to a reference line or mean line.

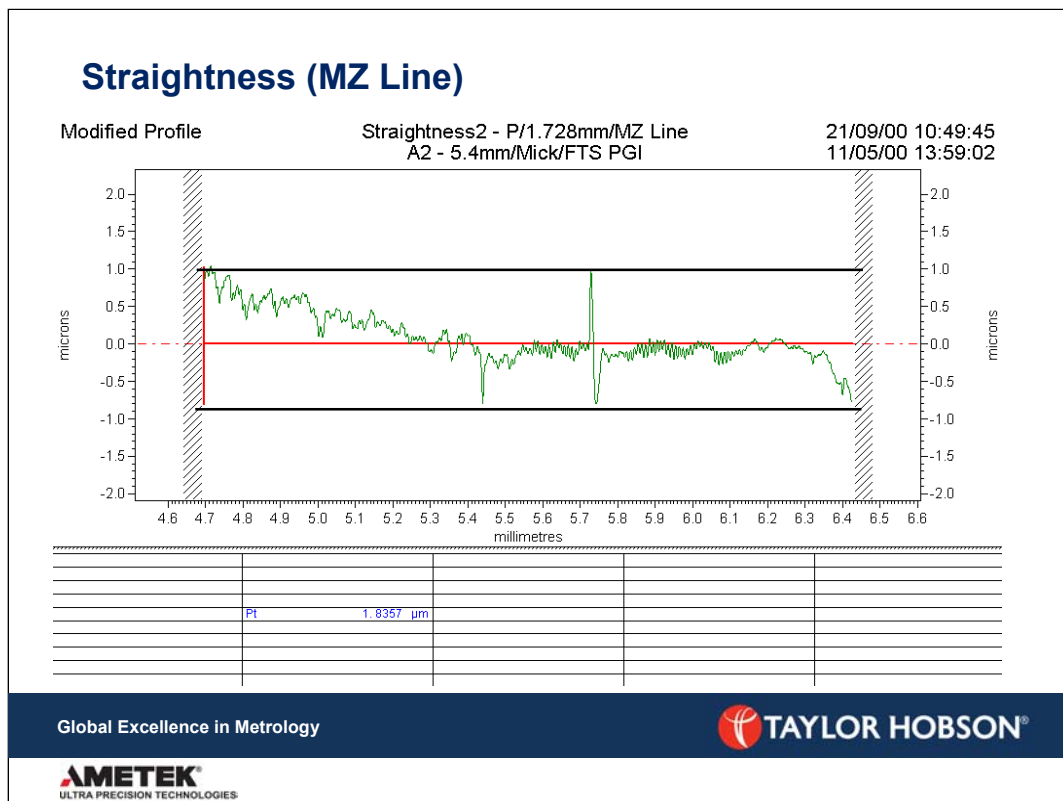
The least squares line is a line which bisects the profile such that the areas above and below this line are equal and are kept to a minimum.

This is shown in the formula:

$a^2 + b^2 + c^2 + d^2 + \dots$  Is at a minimum.



For a straightness result the measured data can be fitted to an LS line the resultant Pt value is the maximum deviation from the LS line i.e the component straightness error.



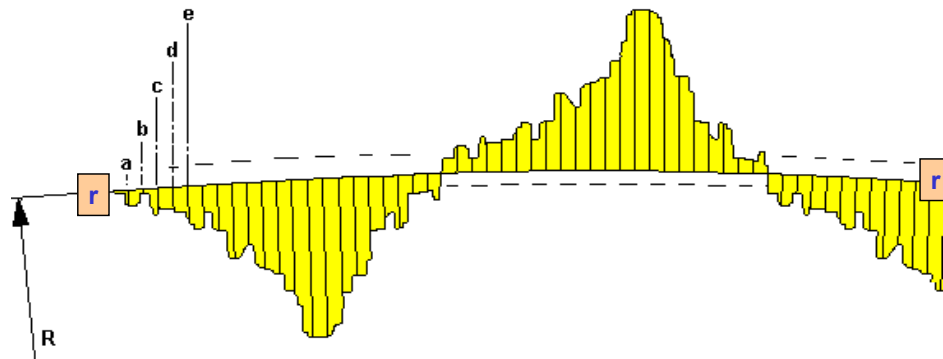
The measured data can also be fitted to an MZ (minimum zone) reference. The minimum zone reference is defined by a pair of straight, parallel lines which just enclose the entire profile such that the distance between the lines (the zone) is a minimum. The displayed reference line is the mean position between these two lines and to which all parameter calculations are referenced. The Pt value displayed is the straightness error. Usually the MZ result will give a smaller straightness error than the LS result over the same profile.

It must be said that using an MZ reference is not as stable as an LS reference due to its susceptibility to random peaks and spikes.

## Form Fit : Least Squares Arc

R = Calculated LS Radius

r-r = LS Arc



$$a^2 + b^2 + c^2 + d^2 + e^2 = \text{minimum}$$

Global Excellence in Metrology

 TAYLOR HOBSON®

 **AMETEK**  
ULTRA PRECISION TECHNOLOGIES

The radius of a measured surface can be determined by fitting an arc to the measurement data. This is positioned such that the sum of the squares of the deviations of the profile from the line of the arc is a minimum, shown as:

$$a^2 + b^2 + c^2 + d^2 + e^2 + \dots$$

The radius of this arc is then calculated.

The principles used are similar to those employed in the calculation of the Least squares Line.

## Accuracy of Radius Measurement

### Factors Affecting Radius Accuracy

#### Component Related

Surface Finish of Component  
Form Error of Component  
Traverse Length / Included Angle

#### Instrument Related

Accuracy of Calibration  
Condition of Stylus  
Traverse Datum Straightness

- ◆ Specify Form Error (Pt) as well as Radius
- ◆ Always Measure within Calibrated Gauge Range

Global Excellence in Metrology



**AMETEK**  
ULTRA PRECISION TECHNOLOGIES

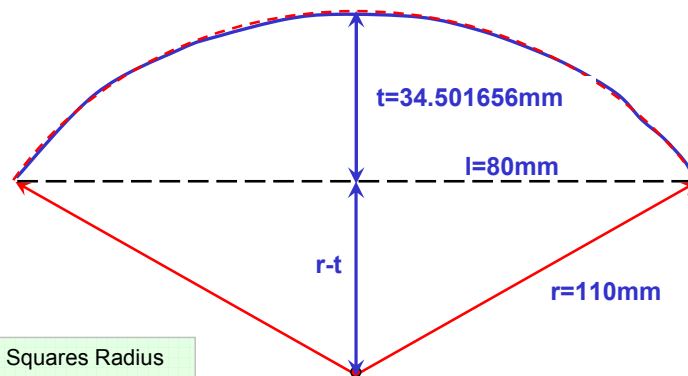
When measuring small radii, the surface roughness of the component and the value of the included angle have a major influence on the accuracy

For larger radii the accuracy depends more on the accuracy of calibration and traverse.

Always specify Pt as well as Radius.



## Accuracy of Radius Measurement - Example



$r$  = Least Squares Radius  
 $t$  = Chordal Height  
 $l$  = Measurement Length/2

Global Excellence in Metrology

 TAYLOR HOBSON®

 **AMETEK**  
ULTRA PRECISION TECHNOLOGIES

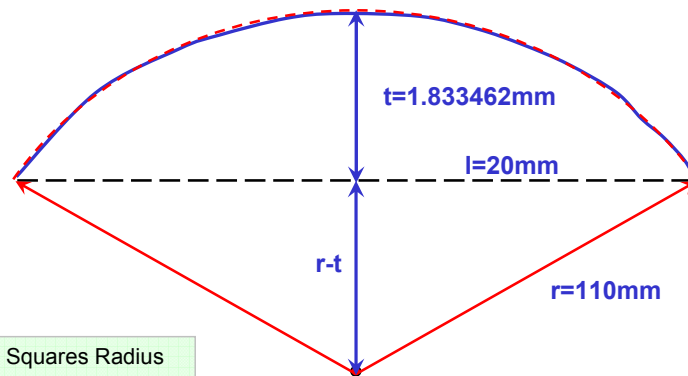
With reference to the diagram above can see a profile (coloured blue) with a slight form error, fitted through this profile is the least squares arc, shown here as a red dotted line.

Using the intersecting chords of a circle theorem we can say that :

So for example a measurement made over a radius of 110mm and a measurement length of 160mm will give a value for  $t$  as follows.

This will make the value for  $t = 34.501656\text{mm}$ .

## Accuracy of Radius Measurement - Example



$r$  = Least Squares Radius  
 $t$  = Chordal Height  
 $l$  = Measurement Length/2

Global Excellence in Metrology

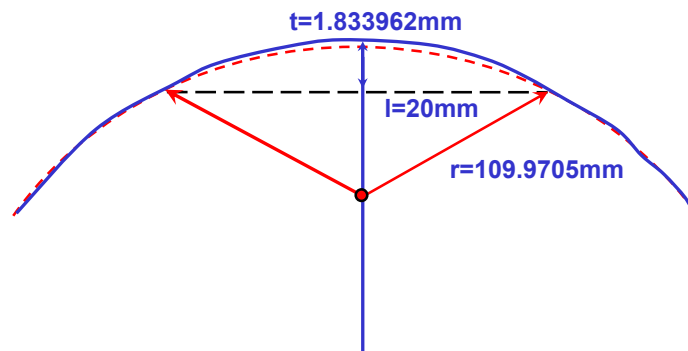
 TAYLOR HOBSON®

 **AMETEK**  
ULTRA PRECISION TECHNOLOGIES

If we now reduce the measurement or assessment length to 40mm for the same least squares arc of the same radius then we can say that:

This will make the value for  $t = 1.833462\text{mm}$ .

## Accuracy of Radius Measurement - Example



$r$  = Least Squares Radius  
 $t$  = Chordal Height  
 $l$  = Measurement Length/2

Global Excellence in Metrology

TAYLOR HOBSON®

AMETEK®  
ULTRA PRECISION TECHNOLOGIES

The profile of this component like all components is not perfect, as we can see from the diagram above, there is an error in form. If we were to calculate a new least squares arc based on the area shown above then the value of  $t$  will change from the calculation in the previous slide which shows the calculation for a true arc. If the value of  $t$  is increased by  $0.5\mu\text{m}$  to represent the new least squares arc calculation based on the form error in the profile, the value for  $t$  will now be changed from 1.833462mm to 1.833962mm.

Substituting this new value in the calculation will give:

$$r = \frac{20^2 + 1.833962^2}{2(1.833962)} \quad r = 109.9705 \text{ mm}$$

In conclusion care must be taken when trying to assess instrument accuracy based on small measurement lengths, the case above is not an error but the true radius at the assessed area. Over small measurement lengths the value of  $t$  has larger effects on radius calculation. Because of these factors when measuring radius and verifying instrument capability it is important to understand that the calibration standards are measured for radius based on the whole or majority of the surface. Standards with slight form errors will have different radius values at different parts of the profile.

## Form Exclusions

- Analysis of Interruptions in Radius (LS Arc)
- Straightness Analysis – Excluding Holes (LS Line)
- Software Levelling

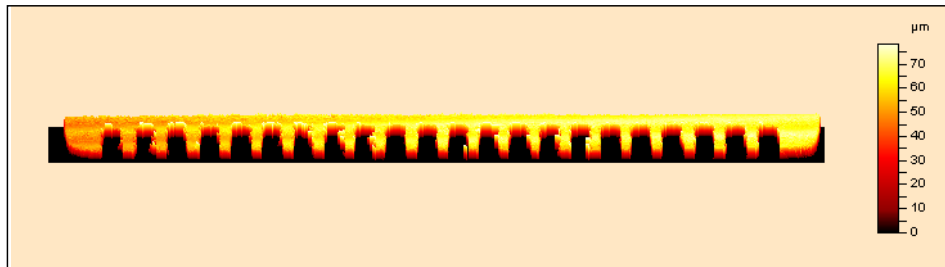
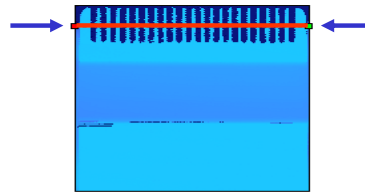
Global Excellence in Metrology



**AMETEK**  
ULTRA PRECISION TECHNOLOGIES

## Form Exclusions - Example

Straightness On Interrupted Surface



Global Excellence in Metrology

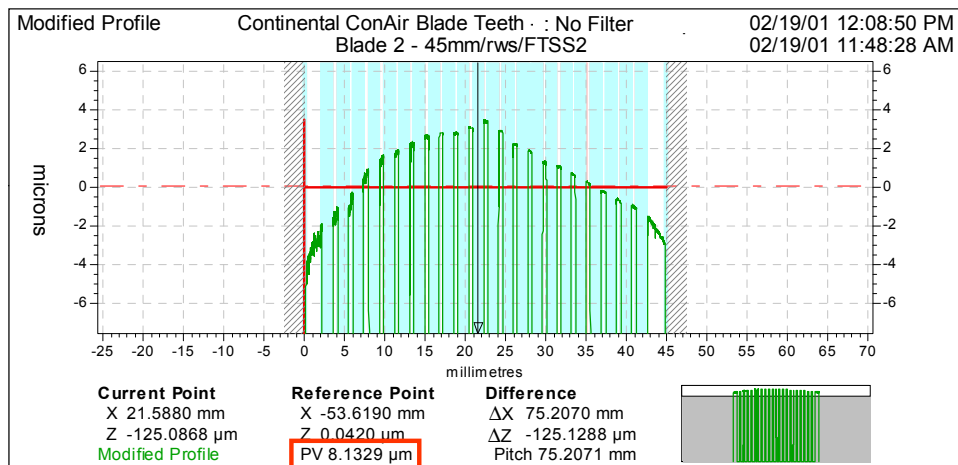
 TAYLOR HOBSON®

 **AMETEK**  
ULTRA PRECISION TECHNOLOGIES

Note use of form fit exclusions (and auto-scale exclusions) to find the straightness of the blade teeth - many interruptions.

Straightness (PV) is 8.13microns.

## Form Exclusions - Example



Global Excellence in Metrology



**AMETEK**  
ULTRA PRECISION TECHNOLOGIES

Note use of form fit exclusions (and auto-scale exclusions) to find the straightness of the blade teeth - many interruptions.

Straightness (PV) is 8.13microns.

## Dimensional Measurement



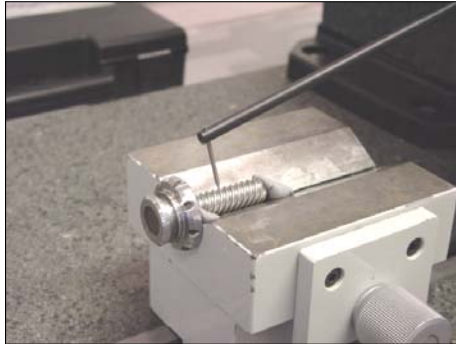
- Angles Between Straight Surfaces
- Pitch, dx and dz between Radius Centres
- Intersections of lines / arcs
- Step Height & Distance Measurement

Global Excellence in Metrology



**AMETEK**  
ULTRA PRECISION TECHNOLOGIES

## Dimensional Measurement - Example



- Profile
- Angle
- Radius

Global Excellence in Metrology



**AMETEK**  
ULTRA PRECISION TECHNOLOGIES



## Summary

- Gauge Range, Resolution and Linearity are important for Form Measurement.
- Parameters such as peak to valley need to be related to a reference line or mean line.
- For a straightness result the measured data can be fitted to an LS line the resultant Pt value is the maximum deviation from the LS line
- The measured data can also be fitted to an MZ (minimum zone) reference.
  - using an MZ reference is not as stable as an LS reference due to its susceptibility to random peaks and spikes
- The radius of a measured surface can be determined by fitting an arc to the measurement data.
  - When measuring small radii, the surface roughness of the component and the value of the included angle have a major influence on the accuracy.
- Form fit exclusions (and auto-scale exclusions) can be used to find the straightness of a surface with interruptions.
- Dimensional Measurements can also be made including distance, step height and angle.

Global Excellence in Metrology



**AMETEK**  
ULTRA PRECISION TECHNOLOGIES

## Contact us

**Material produced by Taylor Hobson Centre of Excellence**

**For more information contact:**

email: [taylor-hobson.cofe@ametek.com](mailto:taylor-hobson.cofe@ametek.com)

or call: +44 116 276 3779

### **Centre of Excellence Services**

For calibration, training and precision metrology beyond the scope of your business expertise, the Taylor Hobson Centre of Excellence has experienced professional metrologists along with state of the art measuring instruments.

### **Metrology Training Courses**

We offer standard and bespoke Training Courses in Surface Finish and Roundness, coupled with contact and non-contact Instrument Operator Training. To improve the understanding and application of Roundness and Surface Finish principles by your operators, inspectors and engineers.

### **Instrument Training**

Without question, the benefits of training are exponentially greater than the cost. When your operators, inspectors and engineers are well versed in the theory and application of metrology they are more confident, more efficient, better informed and more likely to avoid mistakes or misrepresentation of results.

### **Technical Support**

Manned by a team of Experienced Metrologist's, we provide a Case Study or Measurement Report Service alongside a Contract Measurement Service, to help in the correct selection of our metrology systems.

Global Excellence in Metrology

